

①

① Solve the equation $|x| + \sqrt{x+4} - 2 = 0$

- The first thing you need to understand is the absolute value function:

$$|x| = \begin{cases} x & \text{if } x \geq 0 \\ -x & \text{if } x \leq 0 \end{cases}$$

why? Imagine $x = 5 (\geq 0)$. Then, $|x| = |5| = 5$

Imagine $x = -5 (\leq 0)$. Then, $|x| = |-5| = 5$.

As $x = -5$, $|-5| = 5$ can be rewritten as

$$|-5| = -(-5) = 5. \text{ Hence, } |x| = -x \text{ if } x \leq 0$$

- Now that we know the absolute value function, we can clearly see that to solve the proposed equation, we need to follow two paths. Firstly, when $x \geq 0$, the equation will become $x + \sqrt{x+4} - 2 = 0$. Secondly, when $x \leq 0$, the equation will be $-x + \sqrt{x+4} - 2 = 0$.

- Assuming $x \geq 0$, and isolating $\sqrt{x+4}$ in the LHS, we get:

leaving 3 @ netting $\sqrt{x+4} = 2 - x$
L.H.S

- Taking squares in both sides, we get:

$$x+4 = (2-x)^2 \Rightarrow x+4 = 4+x^2-4x$$

- Passing everything to the RHS, we get:

$$0 = x^2 - 5x$$

- Taking x as a common factor, we get:

$$0 = x(x-5)$$

- Hence, either $x=0$ or $x-5=0 \Rightarrow x=5$