

• Cramer's rule:  $\frac{1}{|A|}$

i) we know  $|A| = -0.4 + 0.8\alpha$

ii) Calculate  $|D_y|$ ,  $|D_c|$ ,  $|D_I|$  and  $|D_S|$

$$D_y = \begin{pmatrix} 1 & -1 & -1 & 1 \\ 0 & -1 & 0 & 0 \\ 80 & 1 & 0 & 0 \\ 20 & 0 & 1 & 0 \\ 24 & 0.2 & 0.2 & -1 \end{pmatrix} \quad D_c = \begin{pmatrix} 1 & 0 & -1 & 1 \\ -0.75 & 80 & 0 & 0 \\ -\alpha & 20 & 1 & 0 \\ 0 & 24 & 0.2 & -1 \end{pmatrix} \quad D_I = \begin{pmatrix} 1 & -1 & 0 & 1 \\ -0.75 & 1 & 80 & 0 \\ -\alpha & 0 & 20 & 0 \\ 0 & 0.2 & 24 & -1 \end{pmatrix}$$

$$D_S = \begin{pmatrix} 1 & -1 & -1 & 0 \\ -0.75 & \alpha & 0 & 80 \\ -\alpha & 0 & 1 & 20 \\ 0 & 0.2 & 0.2 & 24 \end{pmatrix}$$

$|D_y|$

$$M_{21}^{D_y} = \begin{vmatrix} -1 & -1 & 1 \\ 0 & 1 & 0 \\ 0.2 & 0.2 & -1 \end{vmatrix} \rightarrow (-1)(1)(-1) + (-1)(0)(0.2) + (1)(0)(0.2) = 1 - 0.2 = \boxed{0.8}$$

$$M_{22}^{D_y} = \begin{vmatrix} 0 & -1 & 1 \\ 20 & 1 & 0 \\ 24 & 0.2 & -1 \end{vmatrix} \rightarrow (0)(1)(-1) + (-1)(0)(24) + (1)(20)(0.2) = 0.2(20) - 20 = -24 = 4 - 20 - 24 = \boxed{-40}$$

$|D_c|$

$$M_{21}^{D_c} = \begin{vmatrix} 0 & -1 & 1 \\ 20 & 1 & 0 \\ 24 & 0.2 & -1 \end{vmatrix} \rightarrow (0)(1)(-1) + (-1)(0)(24) + (1)(20)(0.2) = 0.2(20) - 24 - 20 = \boxed{-40}$$

$$M_{22}^{D_c} = \begin{vmatrix} 1 & -1 & 1 \\ -\alpha & 1 & 0 \\ 0 & 0.2 & -1 \end{vmatrix} \rightarrow \text{Same as } M_{22} \text{ of bigger matrix} = \boxed{-1 + 0.8\alpha}$$

$|D_I|$

$$M_{31}^{D_I} = \begin{vmatrix} -1 & 0 & 1 \\ 1 & 80 & 0 \\ 0.2 & 24 & -1 \end{vmatrix} \rightarrow (-1)(80)(-1) + (0)(0)(0.2) + (1)(1)(24) = 80 + 24 - 16 = \boxed{88}$$

$$M_{33}^{D_I} = \begin{vmatrix} 1 & -1 & 1 \\ -0.75 & 1 & 0 \\ 0 & 0.2 & -1 \end{vmatrix} \rightarrow (1)(1)(-1) + (-1)(0)(0) + (1)(-0.75)(0.2) = -1 - 0.15 + 0.75 = \boxed{-0.4}$$

$|D_S|$

$$M_{21}^{D_S} = \begin{vmatrix} -1 & -1 & 0 \\ 0 & 1 & 20 \\ 0.2 & 0.2 & 24 \end{vmatrix} \rightarrow (-1)(1)(24) + (-1)(20)(0.2) + (0)(0)(0.2) = -24 - 4 + 4 = \boxed{-24}$$

$$M_{22}^{D_S} = \begin{vmatrix} 1 & -1 & 0 \\ -\alpha & 1 & 20 \\ 0 & 0.2 & 24 \end{vmatrix} \rightarrow (1)(1)(24) + (-1)(0)(10) + (0)(-1-\alpha)(0.2) = 24 - 4 - 24\alpha = \boxed{20 - 24\alpha}$$

$$M_{24}^{D_S} = \begin{vmatrix} 1 & -1 & -1 \\ -\alpha & 0 & 1 \\ 0 & 0.2 & 0.2 \end{vmatrix} \rightarrow (1)(0)(0.2) + (-1)(1)(0) + (-1)(-\alpha)(0.2) = 0.2\alpha - 0.2 - 0.2\alpha = \boxed{-0.2}$$

•  $|D_y| = 80 \cdot (-1)^3 \cdot (0.8) + (1)(-1)^4 \cdot (-40) = -80 \cdot (0.8) + (1)(1)(-40) = -64 - 40 = \boxed{-104}$

•  $|D_c| = (-0.75)(-1)^3 \cdot (-40) + (80)(-1)^4 \cdot (-1 + 0.8\alpha) = (-0.75)(-1)(-40) + (80)(1)(-1 + 0.8\alpha) = (0.75)(-40) + (80)(-1) + (80)(0.8\alpha) = -30 - 80 + 64\alpha = \boxed{-110 + 64\alpha}$

•  $|D_I| = (-\alpha) \cdot (-1)^4 \cdot (88) + (20) \cdot (-1)^6 \cdot (-0.4) = (-\alpha)(1)(88) + (20)(1)(-0.4) = \boxed{-88\alpha - 8}$

•  $|D_S| = (-0.75)(-1)^3 \cdot (-24) + (1) \cdot (-1)^4 \cdot (20 - 24\alpha) + (80) \cdot (-1)^5 \cdot (-0.2) = 18 + 20 - 24\alpha - 16 = \boxed{22 - 24\alpha}$