

$$\frac{c'(q) - c(q)/q}{q} = 0$$

$$\Rightarrow c'(q) - c(q)/q = 0$$

$$\Rightarrow \boxed{c'(q) = c(q)/q}$$

Actually, when we minimise the average cost we are just implying that the average cost and the marginal cost should be equal!